#### **Reinforcement Learning**

Odelia Schwartz 2017

## Forms of learning?

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- Unsupervised learning
- Supervised learning
- Reinforcement learning

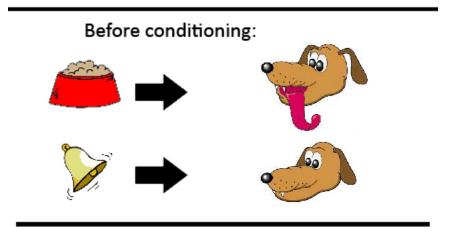
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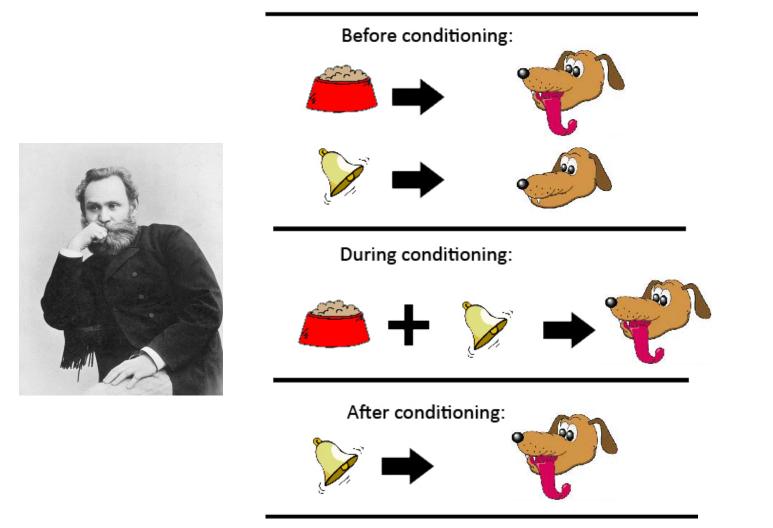
Another active field that combines computation, machine learning, neurophysiology, fMRI

### Pavlov and classical conditioning





# Pavlov and classical conditioning



#### Modern terminology

- Stimuli
- Rewards
- Expectations of reward: behavior is learned based on expectations of reward
- Can learn based on consequences of actions (instrumental conditioning); can learn whole sequence of actions (example: maze)

- Can describe classical conditioning and range of related effects
- Based on simple linear prediction of reward associated with a stimulus (error based learning)
- Includes weight updating as in the perceptron rule we did in lab, but we learn from error in predicting reward

- Minimize difference between received reward and predicted reward
- Binary variable u (1 if stimulus is present; 0 if absent)
- Predicted reward v
- Linear weight w

v = wu

• If stimulus u is present:

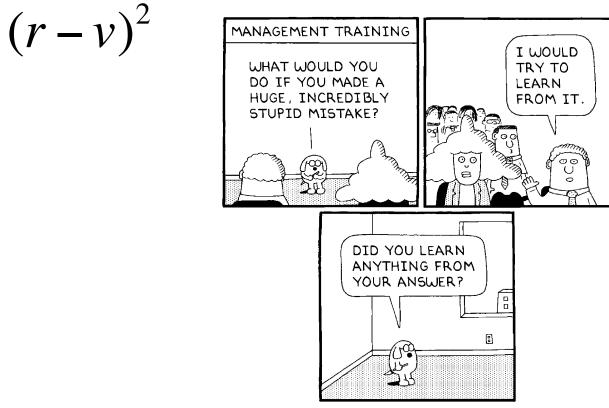
 $\mathcal{V} = \mathcal{W}$ 

based on Dayan and Abbott book

• Minimize squared error between received reward r and predicted reward v:

$$(r-v)^2$$

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In Niv and Schoenbaum 2009

• Minimize squared error between received reward r and predicted reward v:  $(r - v)^2$ 

(average over presentations of stimulus and reward)

• Update weight:

$$w \rightarrow w + \varepsilon (r - v) u$$

 ${\cal E}$  learning rate

Also known as delta learning rule:  $\delta = r - v$ 

• Update weight:

$$w \rightarrow w + \varepsilon (r - v)u$$

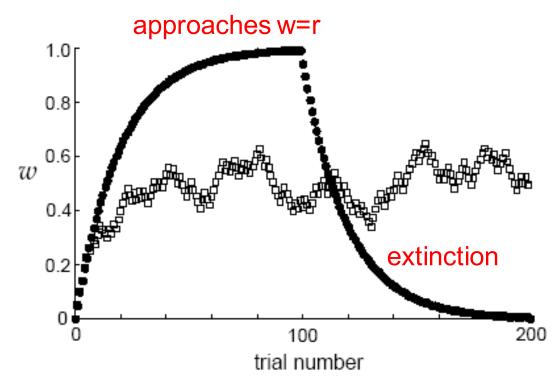
• Simpler notation: if a stimulus is presented at trial n (we'll just take u as 1 and set v to w):

$$v_{n+1} = v_n + \epsilon (r_n - v_n)$$

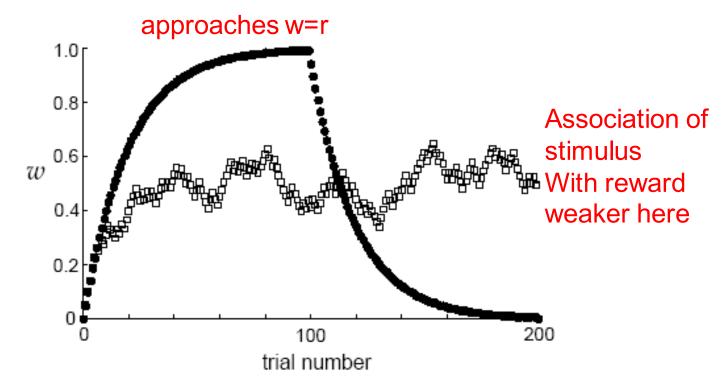
• So if a stimulus is presented at trial n:

$$v_{n+1} = v_n + \epsilon (r_n - v_n)$$

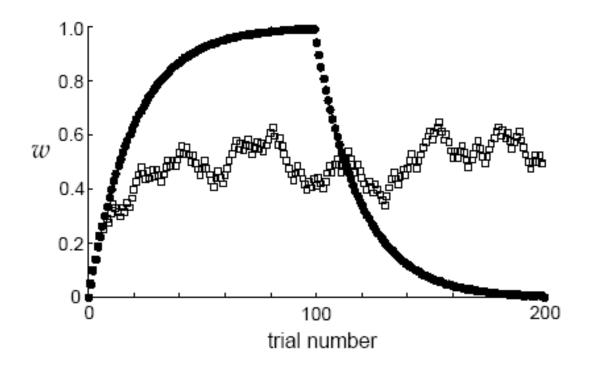
- What happens when learning rate = 1?
- What happens when it is smaller than 1?



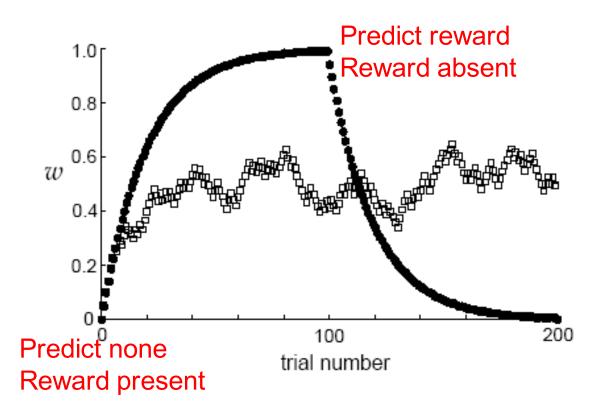
- Solid: First 100 trials: reward (r=1) paired with stimulus; next 100 trials no reward (r=0) paired with stimulus (learning rate .05)
- Dashed: Reward paired with stimulus randomly 50 percent of time



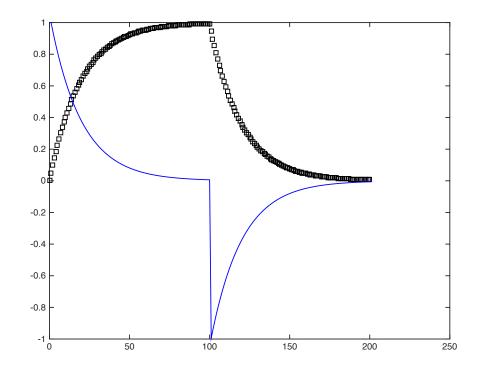
- Solid: First 100 trials: reward (r=1) paired with stimulus; next 100 trials no reward (r=0) paired with stimulus (learning rate .05)
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- Curves show w over time
- What is the predicted reward v and the error (r-v)?

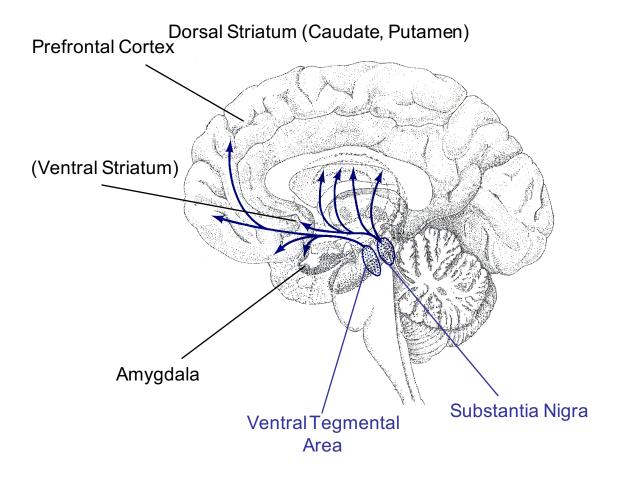


- Curves show w over time
- What is the predicted reward v and the error (r-v)?



- Black curve: v
- Blue curve: (r-v)

#### Dopamine areas



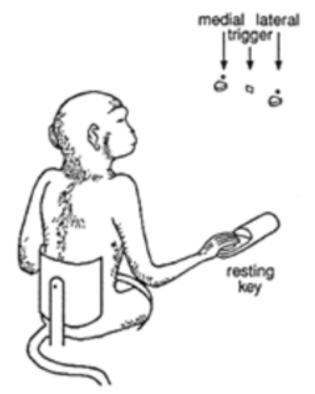
From Dayan slides

Dopamine roles?

Dopamine roles?

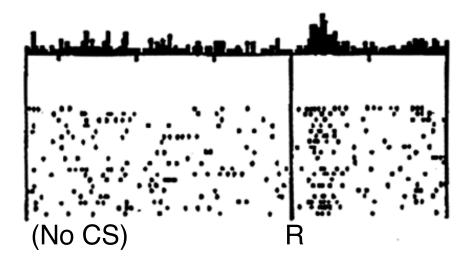
Associated with...

- reward (we'll see prediction error)
- self-stimulation
- motor control (initiation)
- addiction

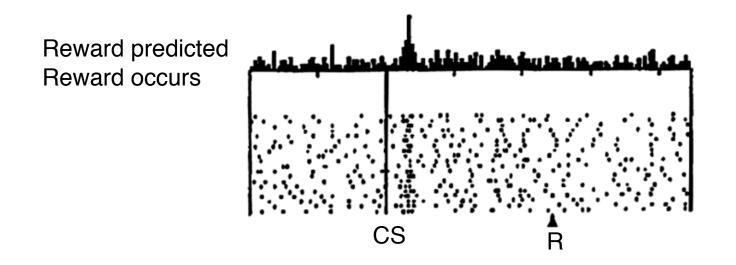


- Monkey trained to respond to light or sound for food and drink rewards (instrumental conditioning)
- Finger on resting key until sound is presented

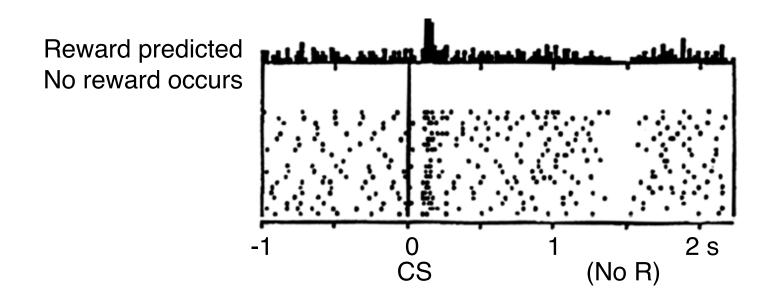
No prediction Reward occurs



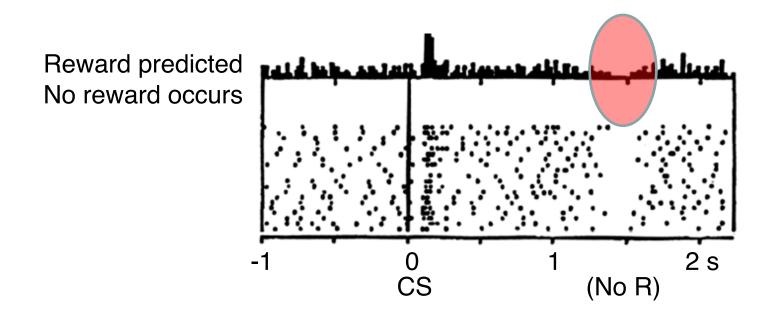
Before learning, reward is given in experiment, but animal does not predict (expect) reward (why is there increased activity after reward?)



After learning, conditioned stimulus predicts reward, and reward is given in experiment (why is activity fairly uniform after reward?)

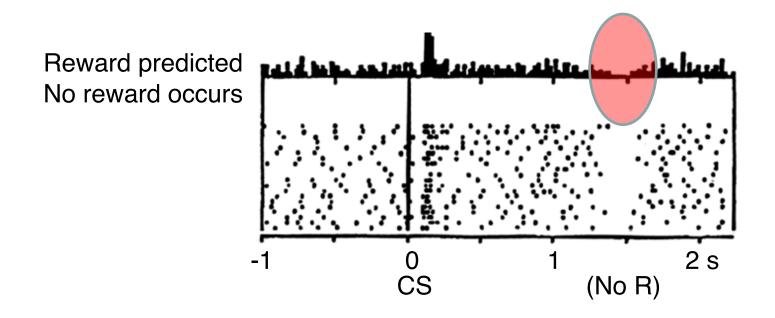


After learning, conditioned stimulus predicts reward so there is an expectation of reward, but no reward is given in the experiment



After learning, conditioned stimulus predicts reward so there is an expectation of reward, but no reward is given in the experiment

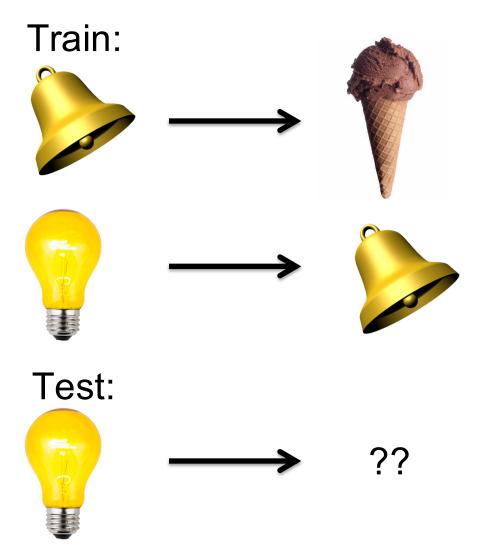
Why is there a dip? What are these neurons doing?



After learning, conditioned stimulus predicts reward so there is an expectation of reward, but no reward is given in the experiment

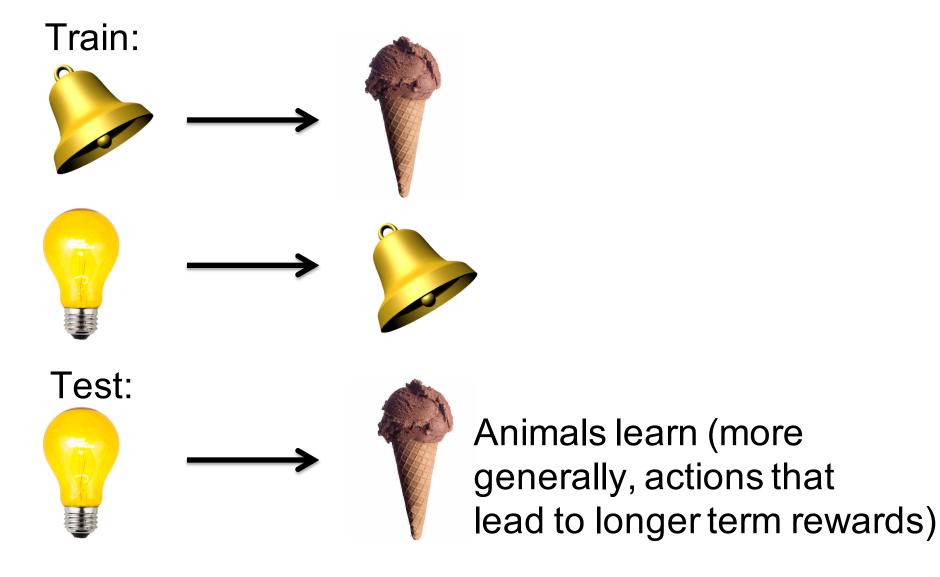
What are these neurons doing? Prediction error between actual and predicted reward (like r-v)

Shortcomings of Rescorla-Wagner: Example: secondary conditioning

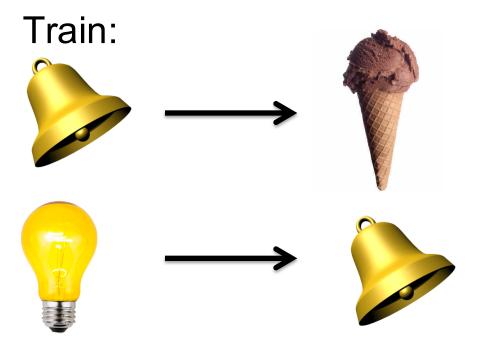


Based on Peter Dayan slides

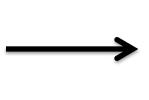
Shortcomings of Rescorla-Wagner: Example: secondary conditioning



Shortcomings of Rescorla-Wagner: Example: secondary conditioning

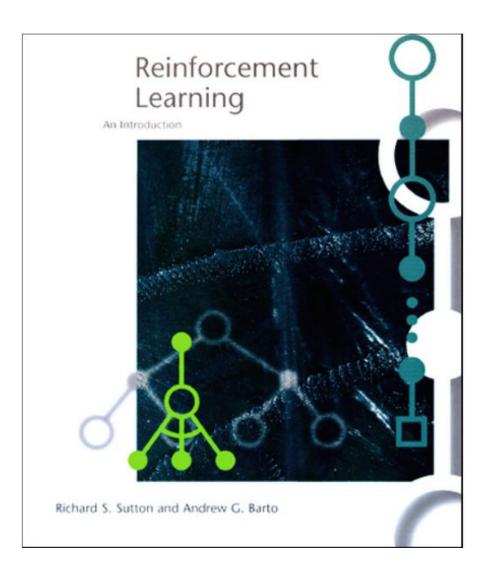


Test:



Rescorla-Wagner would predict no reward; only predicts immediate reward

# 1990s: Sutton and Barto (Computer Scientists)



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• Rescorla-Wagner

VERSUS

• Temporal Difference Learning:

Predict value of future rewards (not just current)

# **Temporal Difference Learning**

• Predict value of future rewards



#### From Dayan slides

# **Temporal Difference Learning**

- Predict value of future rewards
- Predictions are useful for behavior
- Generalization of Rescorla-Wagner to real time
- Explains data that Rescorla-Wagner does not

Based on Dayan slides

### **Rescorla-Wagner**

Want 
$$V_n = r_n$$
 (here n represents a trial)  
Error  $\delta_n = r_n - v_n$ 

$$v_{n+1} = v_n + \varepsilon \delta_n$$

Want 
$$V_t = r_t + r_{t+1} + r_{t+2} + r_{t+3} + \cdots$$

(here t represents time within a trial; reward can come at any time within a trial. Sutton and Barto interpret  $V_t$  as the prediction of total future reward expected from time t onward until the end of the trial)

#### Based on Dayan slides; Daw slides

Want 
$$V_t = r_t + r_{t+1} + r_{t+2} + r_{t+3} + \cdots$$

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Prediction error:

$$\delta_t = (r_t + r_{t+1} + r_{t+2} + r_{t+3}....) - V_t$$

Want 
$$V_t = r_t + r_{t+1} + r_{t+2} + r_{t+3} + \dots$$

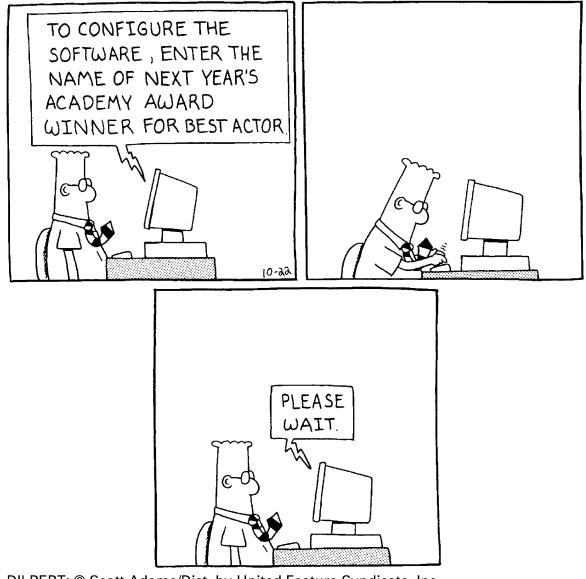
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Prediction error:

$$\delta_t = (r_t + r_{t+1} + r_{t+2} + r_{t+3}....) - V_t$$

Problem??

Based on Dayan slides; Daw slides



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In Niv and Schoenbaum, Trends Cog Sci 2009

Want 
$$V_t = r_t + r_{t+1} + r_{t+2} + r_{t+3} + \dots$$

(here t represents time within a trial)

But we don't want to wait forever for all future rewards...

$$r_{t+1}; r_{t+2}; r_{t+3}....$$

Want 
$$V_t = r_t + r_{t+1} + r_{t+2} + r_{t+3} \dots$$

(here t represents time within a trial)

Recursion "trick":

$$v_t = r_t + v_{t+1}$$

Reward now plus my anticipation now equals total anticipated future

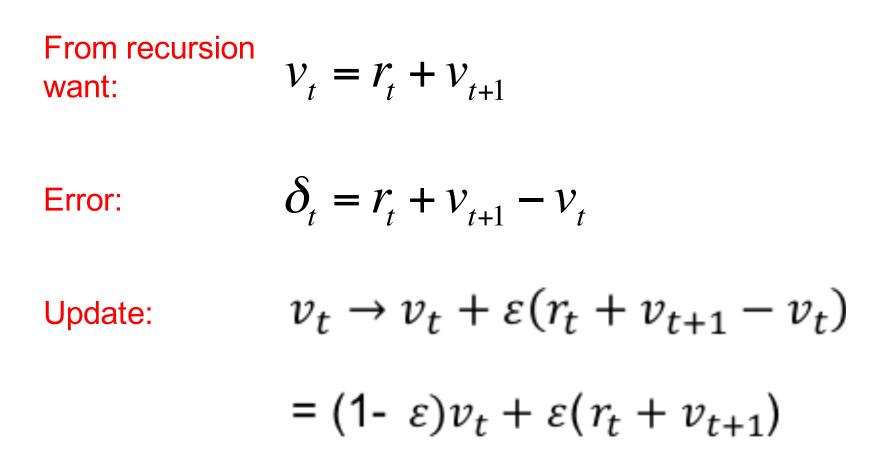
Based on Dayan slides; Daw slides

From recursion 
$$V_t = V_t + V_{t+1}$$
 want:

**Error**:

$$\delta_t = r_t + v_{t+1} - v_t$$

Difference between what I anticipate at time t+1 and what I anticipate at time t



## RV versus TD

• Rescorla-Wagner error: (n represents trial)

$$\delta_n = r_n - v_n$$

Temporal Difference Error: (t is time within a trial)

$$\delta_t = r_t + v_{t+1} - v_t$$

Name comes from!

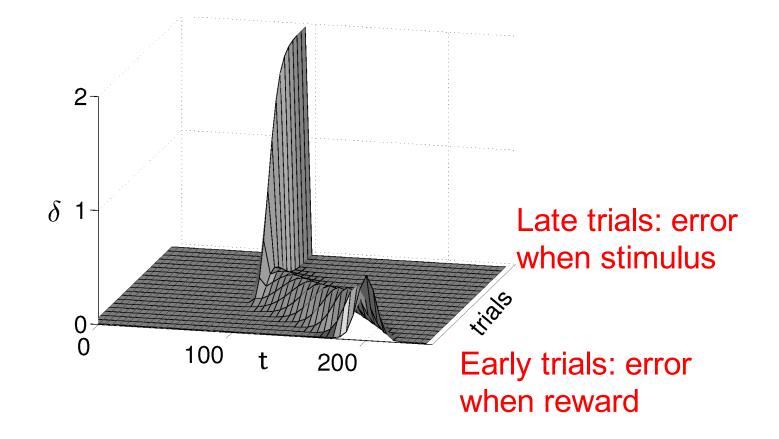
Temporal Difference Error: (t is time within a trial)

$$\delta_t = r_t + v_{t+1} - v_t$$

Name comes from!

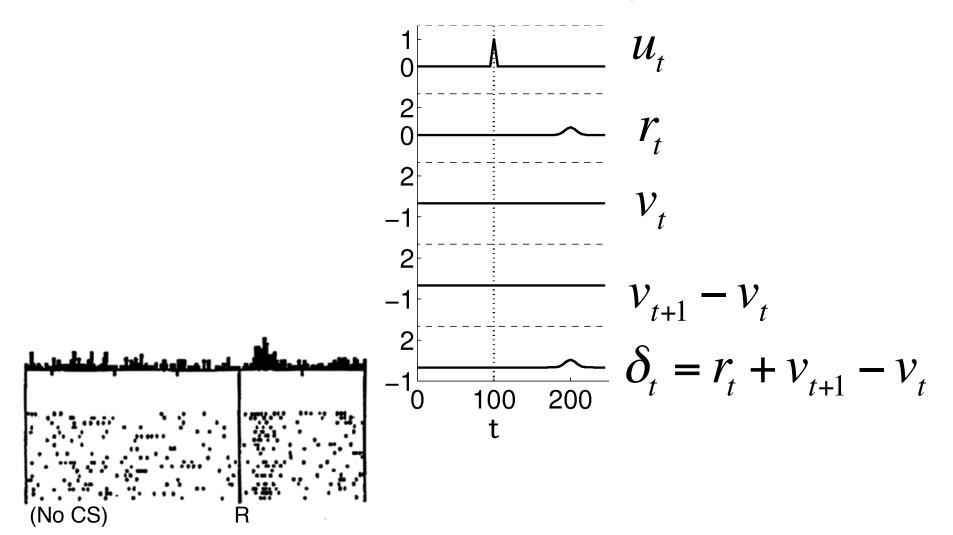
- $V_{t+1} = V_t$  Predictions steady
- $V_{t+1} > V_t$  Got better
- $V_{t+1} < V_t$  Got worse

Based on Daw slides

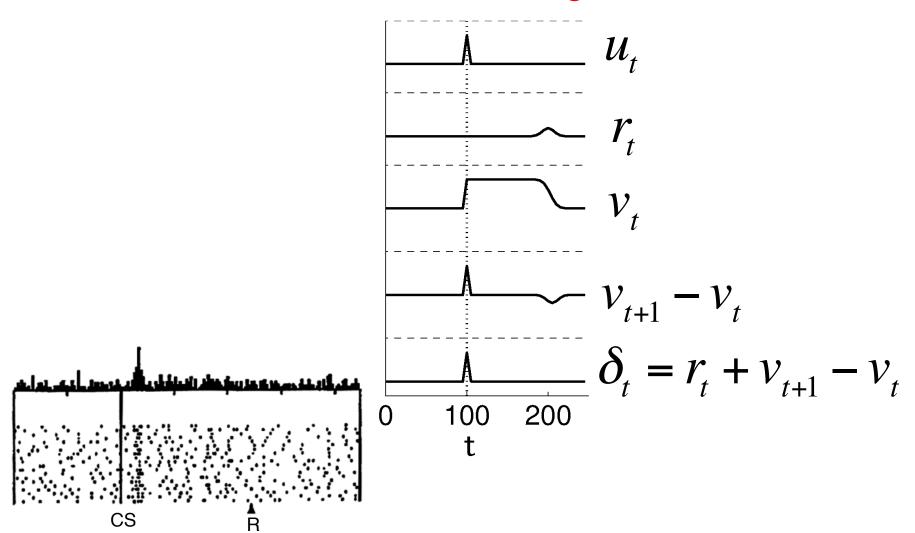


Dayan and Abbott Book: Surface plot of prediction error (stimulus at 100; reward at 200)

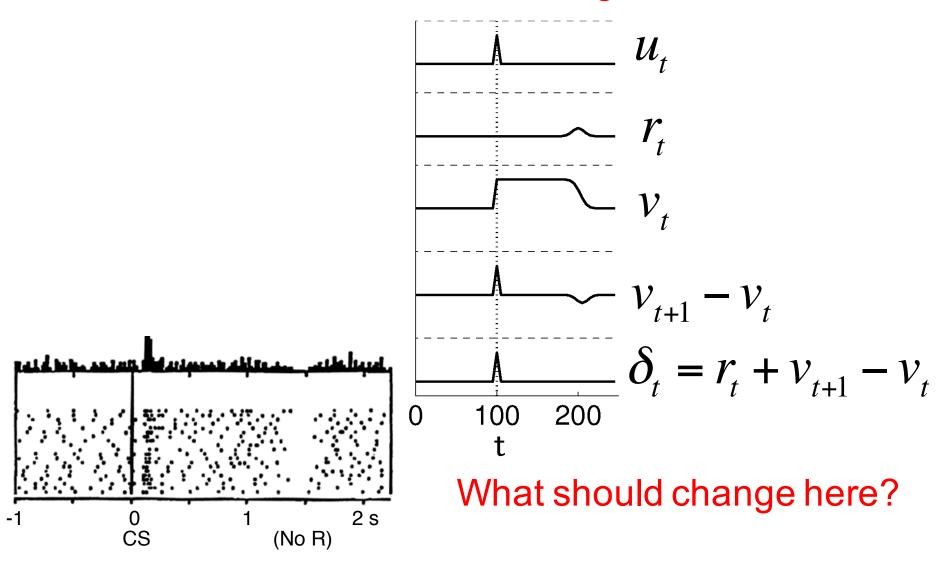
**Before learning** 



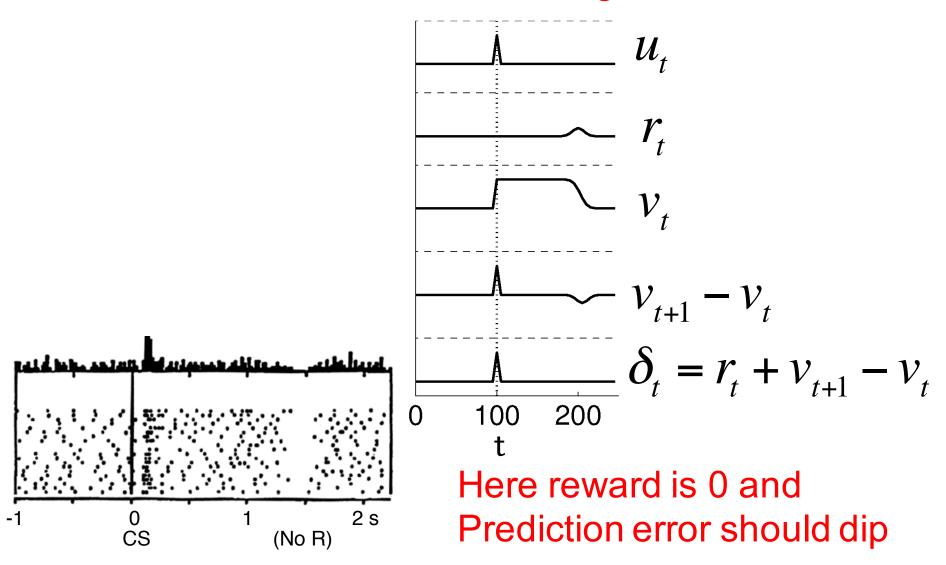
After learning



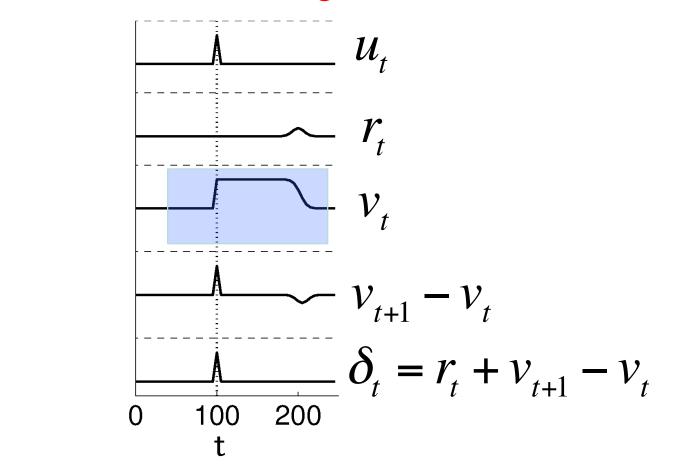
After learning



After learning

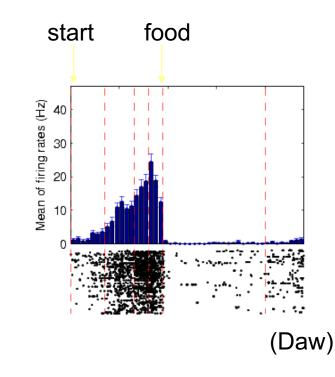


After learning



What about anticipation of future rewards?

Striatal neurons (activity that precedes rewards and changes with learning)



#### What about anticipation of future rewards?

From Dayan slides

## Summary

Marr's 3 levels:

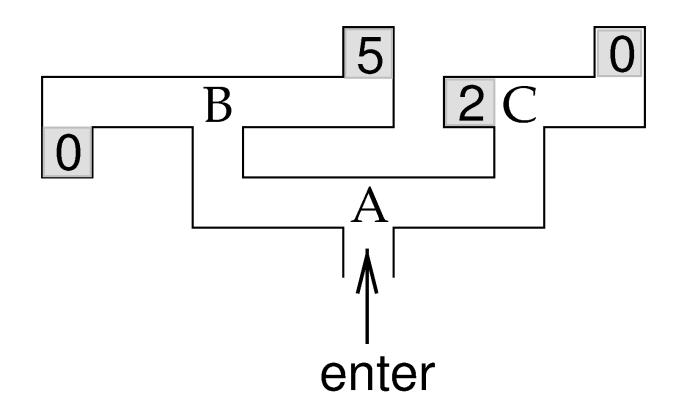
- Problem: Predict future reward
- Algorithm: Temporal Difference Learning (generalization of Rescorla-Wagner)
- Implementation: Dopamine neurons signaling error in reward prediction

Based on Dayan slides

## What else

- Applied in more sophisticated sequential decision making tasks with future rewards
- Foundation of a lot of active research in Machine Learning, Computational Neuroscience, Biology, Psychology

#### More sophisticated tasks



Dayan and Abbott book

#### Recent example in machine learning

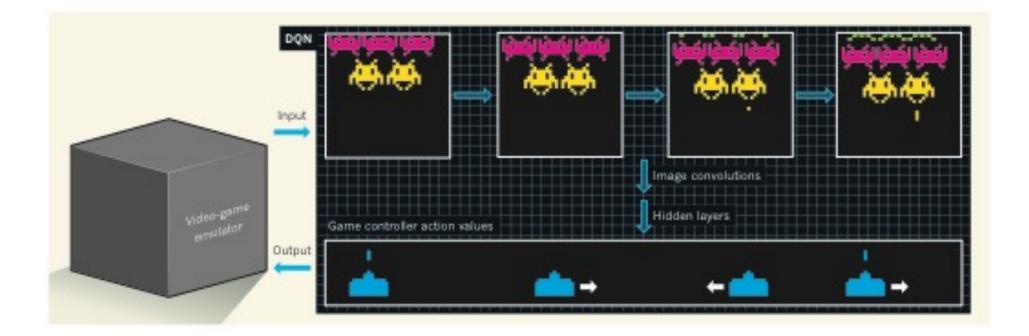
## LETTER

doi:10.1038/nature14236

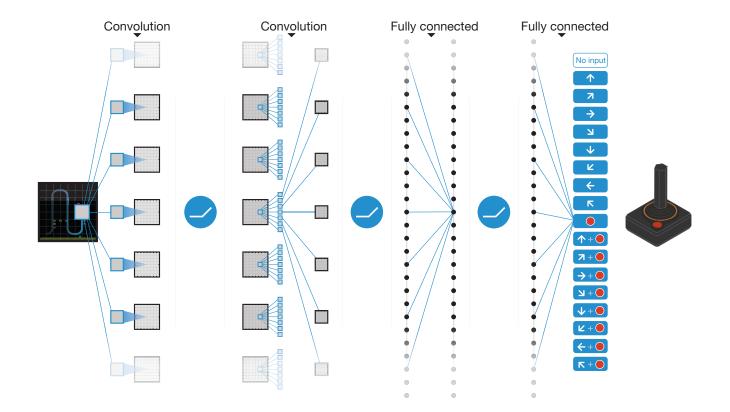
# Human-level control through deep reinforcement learning

Volodymyr Mnih<sup>1</sup>\*, Koray Kavukcuoglu<sup>1</sup>\*, David Silver<sup>1</sup>\*, Andrei A. Rusu<sup>1</sup>, Joel Veness<sup>1</sup>, Marc G. Bellemare<sup>1</sup>, Alex Graves<sup>1</sup>, Martin Riedmiller<sup>1</sup>, Andreas K. Fidjeland<sup>1</sup>, Georg Ostrovski<sup>1</sup>, Stig Petersen<sup>1</sup>, Charles Beattie<sup>1</sup>, Amir Sadik<sup>1</sup>, Ioannis Antonoglou<sup>1</sup>, Helen King<sup>1</sup>, Dharshan Kumaran<sup>1</sup>, Daan Wierstra<sup>1</sup>, Shane Legg<sup>1</sup> & Demis Hassabis<sup>1</sup>

#### Mnih et al. Nature 518, 529-533; 2015



#### Scholkopf. News and Views; Nature 2015



Mnih et al. Nature 518, 529–533; 2015

